Intermediate Mathematical Challenge Wednesday 31 January 2024

E TRAINING CENTRE

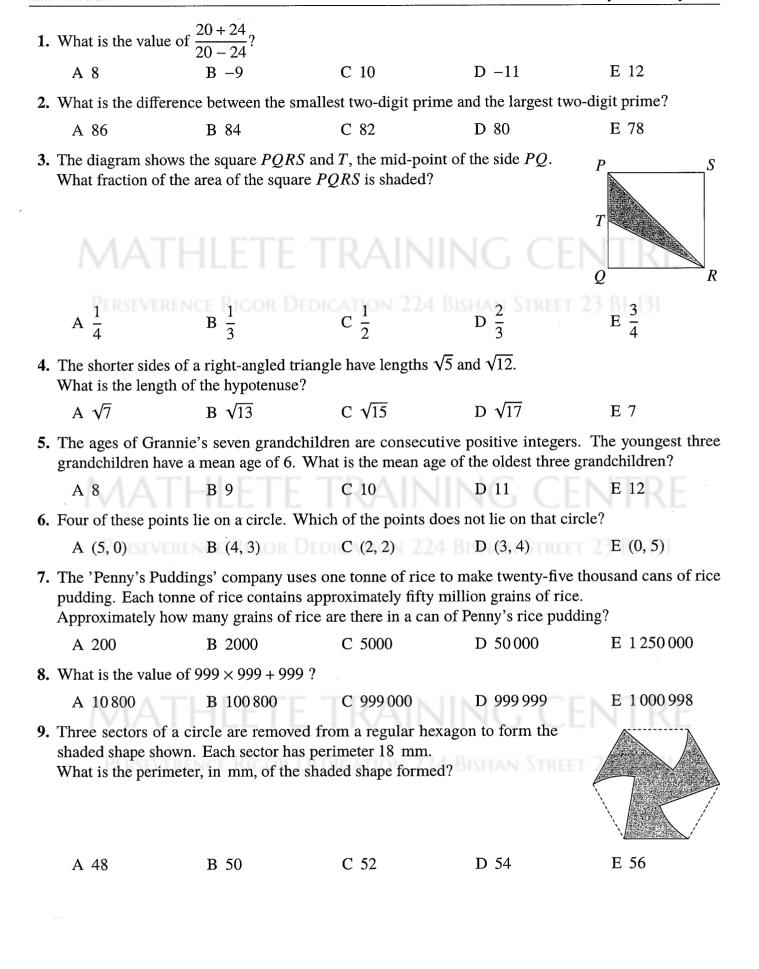
England & Wales: Year 11 or below
Scotland: S4 or below
Northern Ireland: Year 12 or below

Instructions

- 1. Do not open the paper until the invigilator tells you to do so.
- 2. Time allowed: **60 minutes**. No answers, or personal details, may be entered after the allowed time is over.
- 3. The use of blank or lined paper for rough working is allowed; squared paper, calculators and measuring instruments are forbidden.
- 4. Use a B or an HB non-propelling pencil. Mark at most one of the options A, B, C, D, E on the Answer Sheet for each question. Do not mark more than one option.
- 5. Do not expect to finish the whole paper in the time allowed. The questions in this paper have been arranged in approximate order of difficulty with the harder questions towards the end. You are not expected to complete all the questions during the time. You should bear this in mind when deciding which questions to tackle.
- 6. Scoring rules:

5 marks are awarded for each correct answer to Questions 1-15; 6 marks are awarded for each correct answer to Questions 16-25; Each incorrect answer to Questions 16-20 loses 1 mark; Each incorrect answer to Questions 21-25 loses 2 marks.

- 7. Your Answer Sheet will be read by a machine. Do not write or doodle on the sheet except to mark your chosen options. The machine will read all black pencil markings even if they are in the wrong places. If you mark the sheet in the wrong place, or leave bits of eraser stuck to the page, the machine will interpret the mark in its own way.
- 8. The questions on this paper are designed to challenge you to think, not to guess. You will gain more marks, and more satisfaction, by doing one question carefully than by guessing lots of answers. This paper is about solving interesting problems, not about lucky guessing.
- 9. To accommodate candidates sitting at other times, please do not discuss the paper on the internet until **08:00 BST on Friday 2 February**. Candidates in time zones more than 3 hours ahead of GMT must sit the paper on Thursday 1 February (as defined locally).



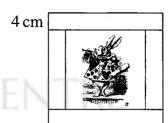
- 10. Which of the following is equal to $\frac{20}{24} + \frac{20}{25}$?

- D $\frac{40}{49}$
- E

40

11. A picture, together with its frame, makes a square of side-length 80 cm. The frame is 4 cm wide.

What percentage of the area of the square is covered by the frame?



A 15%

B 18%

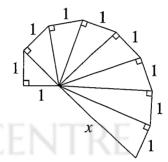
C 19%

D 20%

E 24%

80 cm -

12. What is the length of the line segment marked x?



A $\sqrt{2}$ B 2 C $2\sqrt{2}$ D 3

- 13. When I increase a certain number by 20%, I get twice as much as when I decrease 20 less than the number by 20%. What is that number?
 - A 40
- B 60
- C 80
- D 100

E 120

- **14.** Going clockwise around a quadrilateral, its interior angles are in the ratio 6:7:8:9. Which of the following is a true statement about the quadrilateral?
 - A It has a right angle
- B It is a trapezium

C It is a parallelogram

D It is a kite

E It is cyclic

15. Carrie the cat and Barrie the bat together weigh 4000 g more than Rollie the rat.

Barrie and Rollie together weigh 2000 g less than Carrie.

Carrie and Rollie together weigh 3000 g more than Barrie.

What is the weight, in grams, of Rollie the rat?

- A 250
- B 500
- C 750
- D 1000

E 1250

16. Factorial *n*, written *n*!, is defined by: $n! = 1 \times 2 \times 3 \times \cdots \times n$.

What is the remainder when 1! + 2! + 3! + 4! + 5! + 6! + 7! + 8! + 9! + 10! is divided by 5?

- A 0
- B 1
- C 2
- D 3

E 4

- **17.** What is $4^{(3^2)}$ divided by $(4^3)^2$?
 - A 1
- B 6
- C 16
- D 32

E 64

18.	The point $P(-1,4)$ is reflected in the y-axis to become Q . The point Q is reflected in the line $y=x$ to become R . The point R is reflected in the x-axis to become S . What is the area of quadrilateral $PQRS$?				
	A 4	B $4\sqrt{2} + 2$	C 6	D $4 + 2\sqrt{2}$	E 8
19.	=	to give the same		row, each column an	d each 6 2 x 3
	A 36	В 18	C 12	D 9	E 4
20.	A shop sign says, "T-shirts. Three for the price of two. Equivalent to a saving of £5.50 on each T-shirt." Using this special offer, what is the cost of three T-shirts?				
	A £16.50	B £22	C £31	D £33	E £49.50
21.	with their centres	s at the mid-point emi-circles, as sh	ts of the sides. The	ntical semi-circles drav e four semi-circles ea	1 \ / /
				$D \pi - \sqrt{2}$	
22.	When a cube is cut into two pieces with a single plane cut, two polyhedra are obtained. Which of these polyhedra <i>cannot</i> be obtained in this way?				
	A A polyhedro D A polyhedro		B A polyhedron v E A polyhedron v	_	polyhedron with 6 faces
23.	centre of the circ	le is the point P , v	where $PA = PO$.	d diameter <i>AB</i> . The as of the semicircle?	A O B
	A 4:9	В 3:8	C 3:7	D 2:5	E 1:2
24.	the hexagon. Jay going clockwise	haded pentagon haded pentagon had Kay walk and Kay anticlock	RSTPQ is one quare round the hexagon	from P to Q , Jay	V = P T $V = Q R$

25. A gold coin is worth x% more than a silver coin. The silver coin is worth y% less than the gold coin. Both x and y are positive integers. How many possible values for x are there?

C 3:5

A 0

A 1:2

B 3

B 2:3

C 6

D 9

D 4:7

E 12

E 5:8